



Article

Broadband Optical Constants and Nonlinear Properties of SnS₂ and SnSe₂

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Abstract: SnS₂ and SnSe₂ have recently been shown to have a wide range of applications in photonic and optoelectronic devices. However, because of incomplete knowledge about their optical characteristics, the use of SnS₂ and SnSe₂ in optical engineering remains challenging. Here, we addressed this problem by establishing SnS₂ and SnSe₂ linear and nonlinear optical properties in the broad (300–3300 nm) spectral range. Coupled with the first-principle calculations, our experimental study unveiled the full dielectric tensor of SnS₂ and SnSe₂. Furthermore, we established that SnS₂ is a promising material for visible high refractive index nanophotonics. Meanwhile, SnSe₂ demonstrates a stronger nonlinear response compared with SnS₂. Our results create a solid ground for current and next-generation SnS₂- and SnSe₂-based devices.

Keywords: two-dimensional materials; optical constants; dielectric properties; refractive index; nanophotonics; spectroscopic ellipsometry; second harmonic generation

1. Introduction

Van der Waals materials have emerged as a promising building block for next-generation optical and electronic devices [1–8]. Their planar structure [9,10] and the outstanding compatibility with existing manufacturing techniques [11–15] make such materials ideal for integration into modern industrial and scientific devices. Among layered materials, graphene [16], MoS₂ [17], and hBN [18] have received the most attention, as they were the first [19–21] to catch researchers' interest during the “two-dimensional” revolution [22] in material science. However, the number of known layered materials has increased exponentially over the last decade, with more than 1000 layered compounds being isolated and identified [23]. As a result, their properties are largely unexplored, which considerably impedes their application. In particular, the optical properties of tin-based dichalcogenides SnS₂ and SnSe₂ [24,25] are mostly unknown, with rare reports [26–30] on their absorption properties. Nonetheless, SnS₂ and SnSe₂ have already demonstrated their huge potential in optoelectronic applications, such as field-effect transistors [31–33], solar cells [34,35], saturable absorbers [36–38], photonic crystals [39,40], and photodetectors [41,42]. Hence, broadband linear and nonlinear optical

properties are highly desired for the acceleration of the development of SnS₂ and SnSe₂-based devices.

Here, the objective of the present work is the comprehensive optical characterization of SnS₂ and SnSe₂. Using spectroscopic ellipsometry and first-principle calculations, we determine the full broadband dielectric tensor of SnS₂ and SnSe₂ from ultraviolet to mid-infrared wavelengths (300–3300 nm). The results demonstrate a high dielectric response ($n > 3$) with zero losses in a wide spectral range: 560–3300 nm for SnS₂ and 1300–3300 nm for SnSe₂. Moreover, we measured the second-order nonlinear optical susceptibility of SnS₂ and SnSe₂ at wavelengths ranging from 750 to 1050 nm. Finally, our results revealed that SnS₂ is a high refractive index material, which fills the important gap in the visible spectrum between bandgap energies of GaP and TiO₂, which makes SnS₂ a promising material for all-dielectric nanophotonics.

2. Results and Discussion

2.1. Surface and Structural Morphology Study

Thin films of SnS₂ and SnSe₂ were synthesized by the chemical vapor deposition (CVD) method and transferred on a quartz substrate. Figure 1a schematically illustrates the crystal structure of 1T-SnS₂ or SnSe₂ viewed along *c*-axis and the *a*-axis. This crystal configuration is the most common atoms' arrangement for SnS₂ and SnSe₂, where layers stack directly above one another [43,44]. Optical microscopy photographs in Figure 1b,f show the uniform substrate's coverage of synthesized SnS₂ and SnSe₂ films. Likewise, scanning electron microscopy (SEM) images in Figure 1c,g confirm the films' full-area coverage and homogeneity at the microscale. In addition, we checked the films' surface by atomic force microscopy (AFM), demonstrating an atomically smooth surface with root mean square (RMS) roughness of less than 1.6 nm and 0.5 nm for SnS₂ and SnSe₂, respectively. Ultimately, we accurately measured the films' thickness via AFM topographical scans (Figure 1e,i). They yielded 20.0 ± 1.8 nm and 6.5 ± 0.7 nm thicknesses for SnS₂ and SnSe₂ films, correspondingly.

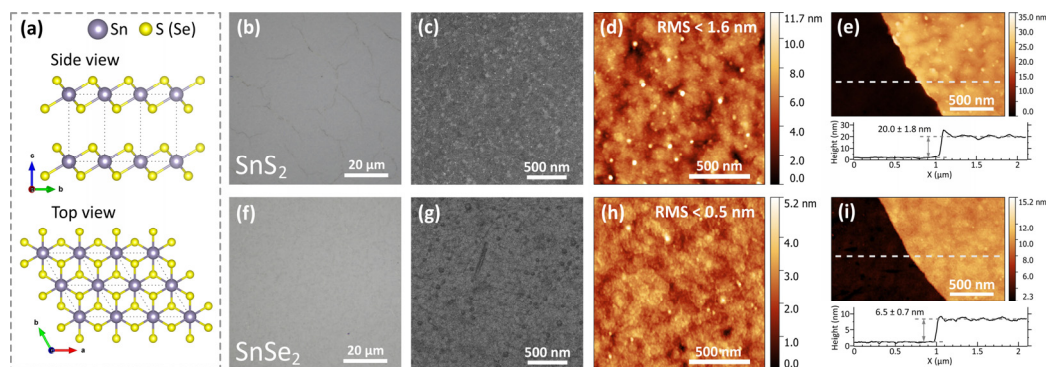


Figure 1. Morphology of SnS₂ and SnSe₂. (a) Crystal lattice structure of 1T-SnS₂ (or 1T-SnSe₂) [44], optical microscopy images of (b) SnS₂ and (f) SnSe₂. SEM images of (c) SnS₂ and (g) SnSe₂. AFM scan images of (d) SnS₂ and (h) SnSe₂. AFM thickness measurements of (e) SnS₂ and (i) SnSe₂ films with characteristic step height profiles.

2.2. Analysis of the Crystal Structure and Raman Characterization

In nature, SnS₂ and SnSe₂ exist in several phase modifications [45,46], including 1T, 2H, 4H, and 18R polytypes. To identify the phase of our samples, we performed X-ray diffraction (XRD), whose spectra are displayed in Figure 2a,b. According to the Joint Committee on Powder Diffraction Standards (card No. 23-0677 and 89-2939) and previous publications [27,47,48], the obtained XRD patterns reveal the hexagonal lattice configuration, which could be 1T or 2H, for SnS₂ and SnSe₂ with lattice parameters $a = b = 3.6486$ Å and $c = 5.8992$ Å for SnS₂ and $a = b = 3.811$ Å and $c = 6.137$ Å for SnSe₂.

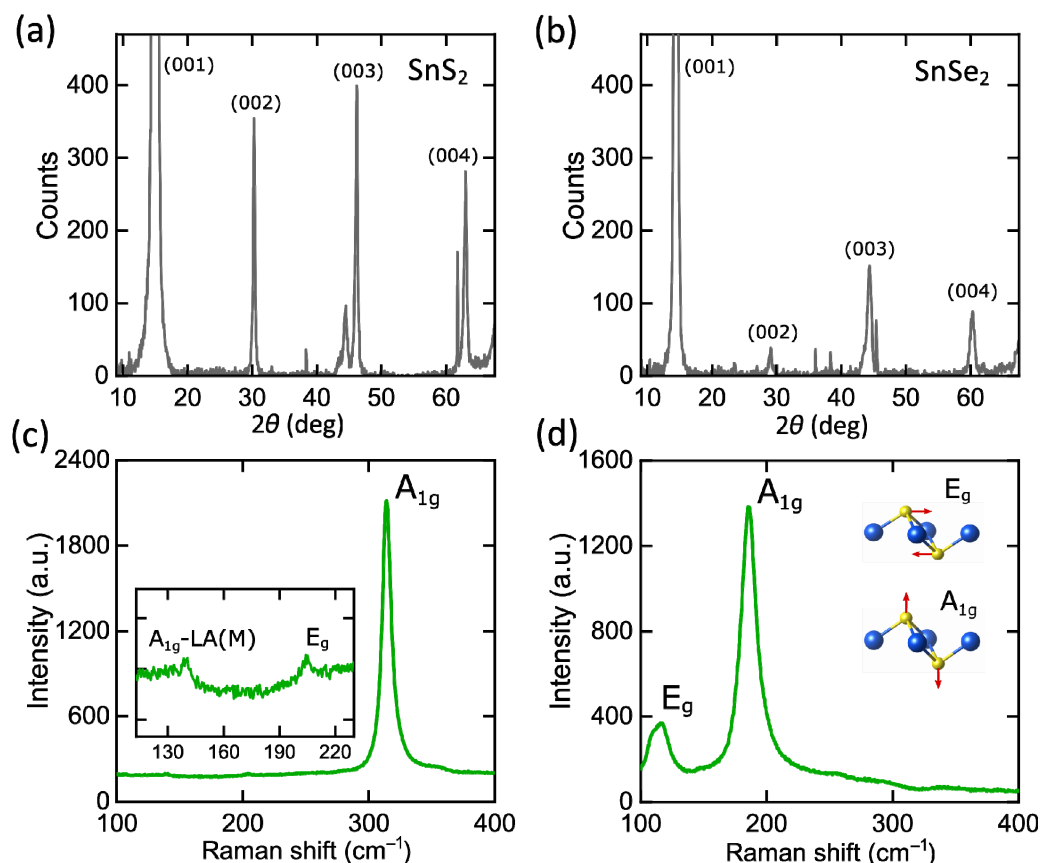


Figure 2. Structural characterization of SnS₂ and SnSe₂. XRD patterns of (a) SnS₂ and (b) SnSe₂. Raman spectra for (c) SnS₂ and (d) SnSe₂ thin films.

Aside from XRD characterization, we utilized Raman spectroscopy at 532 nm excitation wavelength (Figure 2c,d) to distinguish between two hexagonal configurations, 1T and 2H. Raman spectrum of SnS₂ reveals out-of-plane vibration mode A_{1g} at ~314 cm⁻¹ and in-plane vibration of E_g at ~205 cm⁻¹, corresponding to 1T polytype [44,49,50]. Similar to SnS₂, SnSe₂ Raman spectrum has two characteristic phonon modes: A_{1g} mode at ~185 cm⁻¹ and E_g mode at ~116.5 cm⁻¹, associated with 1T-phase [36,51]. Moreover, Raman spectra at numerous locations of our samples demonstrate the same A_{1g} and E_g peak positions, additionally validating the homogeneity of the studied SnS₂ and SnSe₂ thin films.

2.3. Optical Properties of SnS₂ and SnSe₂ Films

We investigated broadband optical constants of SnS₂ and SnSe₂ films through spectroscopic ellipsometry. We employed a two-layer optical model for ellipsometry data analysis: quartz substrate with SnS₂ or SnSe₂ film with the thickness determined from AFM (Figure 3e,i). Similar to other TMDCs [52,53], we describe SnS₂ and SnSe₂ dielectric function by the Tauc–Lorentz oscillator model (see Methods) [54,55]. Figure 3a,b shows the resulting optical constants *n* and *k* for SnS₂ and SnSe₂ films. Interestingly, we did not observe excitons for SnS₂ and SnSe₂, which can be explained by their indirect bandgap, in contrast, to the direct bandgap in MoS₂ and WS₂ [56,57]. Apart from the dielectric function, Tauc–Lorentz oscillator parameters allow us to obtain the positions of critical points of joint density of states: 3.91 eV (317 nm) for SnS₂; 2.87 eV (432 nm) and 3.98 eV (311 nm) for SnSe₂. Furthermore, SnS₂ and SnSe₂ both have zero absorption (*k* ~ 0) at a broad wavelength range, starting from 560 and 1300 nm (Figure 3a,b), respectively. For reference, we also plotted in Figure 3a,b refractive indices and bandgap transitions of SnS₂ and SnSe₂, determined by Domingo and coworkers [26]. As expected, the fundamental absorption edge coincides with the forbidden indirect transitions (Figure 3a,b), supporting our results in Figure 3a,b.

For additional verification, we also measured the transmittance spectra of our samples (Figure 3c,d) and compared them with the transfer matrix calculations [58], based on optical constants from Figure 3a,b. Evidently, calculated and measured transmittance agree well, thereby validating our n and k in Figure 3a,b.

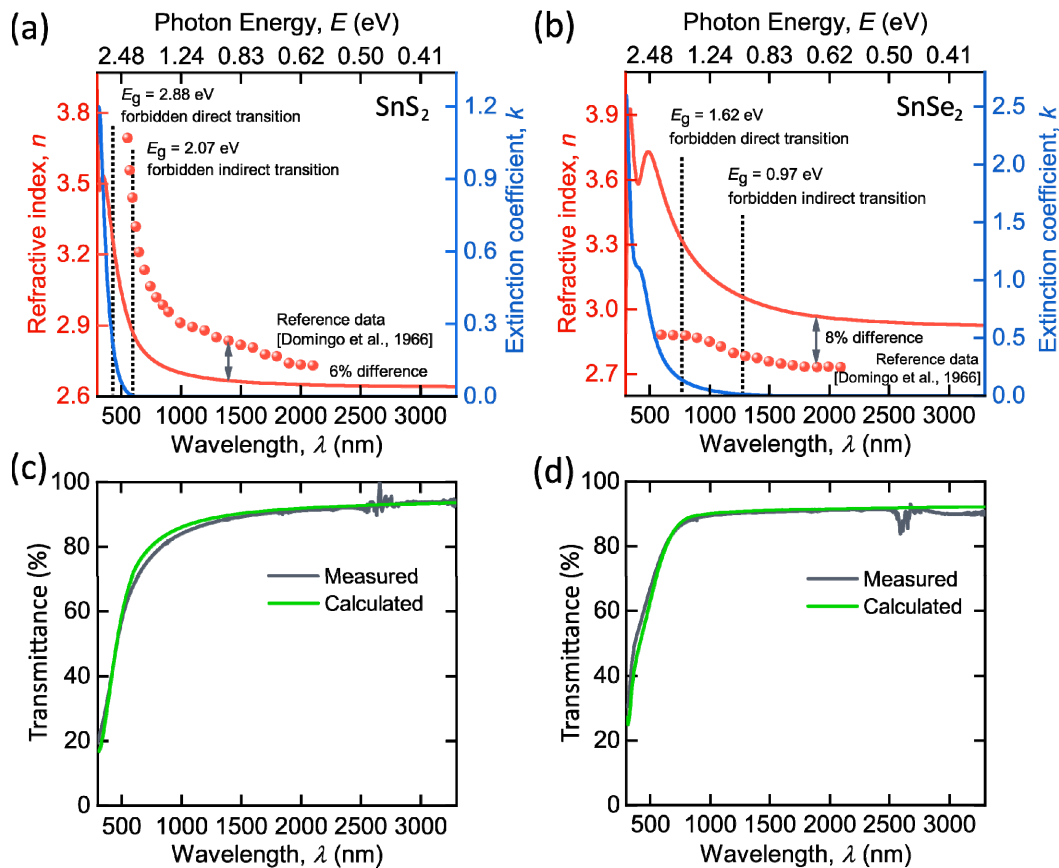


Figure 3. Linear optical properties of SnS₂ and SnSe₂. Dielectric function of (a) SnS₂ and (b) SnSe₂. For comparison, we included refractive indices (red circles) and electronic transitions (dashed lines) determined by Domingo et al. [26]. Measured and calculated transmittance for (c) SnS₂ and (d) SnSe₂ on quartz. Tabulated optical constants for SnS₂ and SnSe₂ are collected in Table A1.

To retrieve the full dielectric tensor, we leveraged first-principle calculations (Methods). Figure 4 shows the resulting refractive index and extinction coefficient along the ab -plane (n_{ab} and k_{ab}) and c -axis (n_c and k_c). The first-principle calculations reproduce the shape of the experimental dielectric function and render the major optical features: a wide zero-absorption spectral range and high dielectric response. However, first-principle calculations overestimate values of dielectric function since the computations were performed assuming the ideal crystalline structure, whereas the studied CVD-grown films have a polycrystalline structure. Nevertheless, first-principle calculations provide access to the full dielectric permittivity tensor, allowing us to estimate the anisotropic optical properties, which are the most noticeable for SnS₂ with birefringence $\Delta n = n_{ab} - n_c \approx 0.3$ and almost negligible for SnSe₂. In contrast, ellipsometry is nearly insensitive to optical constants along the c -axis, as explained by Ermolaev and colleagues [56,59]. Thus, our computations reveal for the first time the optical anisotropy in SnS₂ and SnSe₂, which could be relevant in next-generation anisotropic nanophotonics [60].

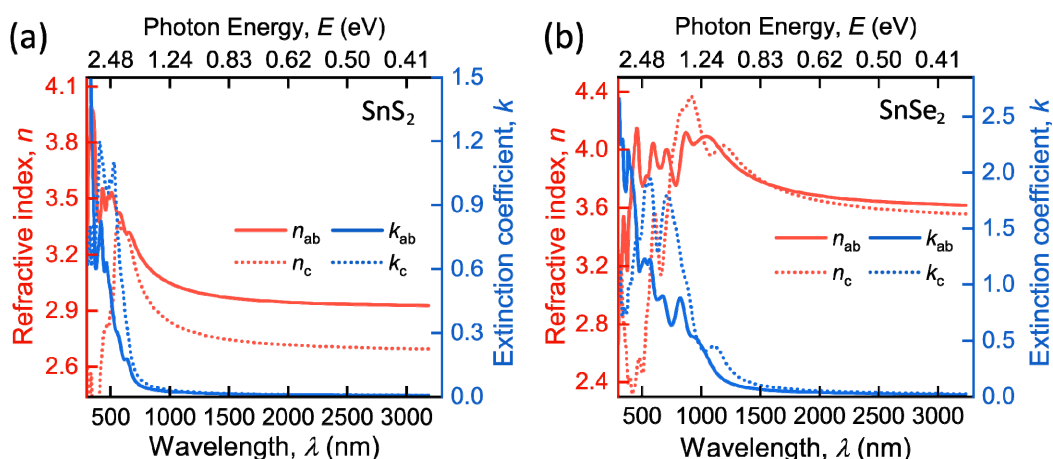


Figure 4. First-principle calculations of SnS₂ and SnSe₂. Optical constants for (a) SnS₂ and (b) SnSe₂, including in-plane n_{ab} , k_{ab} and out-of-plane n_c , k_c parts of dielectric tensor.

In the light of the rapid development of nonlinear optical devices based on SnS₂ and SnSe₂ [36,37,61], we also measured their nonlinear optical response (Figure 5). Specifically, we measured the second harmonic generation (SHG) in transmission geometry using 150 fs laser pulses focused into a 50 μm spot in diameter (see Methods). Figure 5a shows the SHG power dependence with the expected slope of 2 (2.01 ± 0.02 for SnS₂ and 2.02 ± 0.04 for SnSe₂), confirming the second-order nonlinear process and the absence of saturation effects. SHG spectra of SnS₂ and SnSe₂ are shown in Figure 5b. For SnSe₂, SHG resonance is at 415 nm (2.98 eV), associated with the 2 photon direct transition at the critical point (2.87 eV) found above from ellipsometry measurements. The presence of SH signal at large pump wavelengths indicates the contribution of direct transitions with lower energies, meaning that the direct transition of SnSe₂ is less than 2.36 eV. In contrast, for SnS₂, the SH signal is negligible at large wavelengths. Therefore, the SHG resonance observed at the SH wavelength of 420 nm (2.95 eV) can be associated with the lowest energy direct transition of SnS₂ in agreement with Domingo and colleagues' work [26].

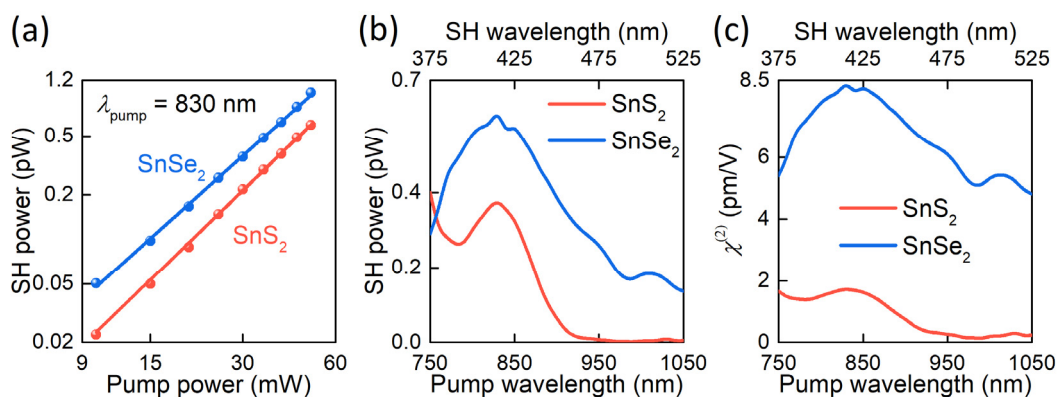


Figure 5. Nonlinear optical properties of SnS₂ and SnSe₂. (a) Power-dependent nonlinear optical response of SnS₂ and SnSe₂ thin films, plotted in double logarithmic scale, and its linear approximation with slope $p = 2.01 \pm 0.02$ for SnS₂ and $p = 2.02 \pm 0.04$ for SnSe₂. Pump wavelength is 830 nm. (b) SHG spectroscopy of SnS₂ (red line) and SnSe₂ (blue line) thin films at 40 mW pump power. (c) Wavelength-dependent, second-order, nonlinear optical susceptibility of SnS₂ (red line) and SnSe₂ (blue line).

To calculate the nonlinear optical susceptibility, we implemented the method, described in Boyd's book [62]. The technique relies on the following equation for the average power of SHG transmitted through sample:

$$P(2\omega) = \frac{16\sqrt{2}|\chi^{(2)}|_2\pi SP^2(\omega)L^2}{\epsilon_0 r^2 f \tau c n_\omega^2 n_{2\omega} \lambda^2} \sin^2\left(\frac{\Delta k L}{2}\right) \quad (1)$$

where $\chi^{(2)}$ is a nonlinear optical susceptibility, $S = 0.94$ is the shape factor for Gaussian pulses, ϵ_0 is the permittivity of vacuum, c is the speed of light, $f = 80$ MHz is the pulse repetition rate, $\tau = 150$ fs is the pulse duration, $r = 25$ μm is the focal spot radius, L is a sample thickness, λ is a pump wavelength, Δk is the wavevectors mismatch of the pump and SH waves, n_ω and $n_{2\omega}$ are refractive indices of material at pump and harmonic wavelengths, and $P(\omega)$ and $P(2\omega)$ are average power of the pump and the second harmonic radiation, respectively. In our case, the coherence length $L_{coh} = \lambda / (4n_{2\omega} - 4n_\omega)$ of the observed processes is several hundred nanometers (from 300 nm to 900 nm for SnS₂ and from 450 to 600 nm for SnSe₂), which significantly exceeds the thickness of the films (Figure 1e,f). Thus, we can assume that the SHG is phase-matched and, hence, $\sin^2(\Delta k L / 2) = 1$. It allows us to evaluate SnS₂ and SnSe₂ nonlinear optical susceptibility, displayed in Figure 5c.

Finally, we want to underline that SnS₂ is a promising material for all-dielectric nanophotonics [63,64], demanding a high refractive index and low absorption. As shown in Figure 6, SnS₂ meets both requirements since it possesses a refractive index $n \approx 2.8$ and zero extinction in the visible and infrared ranges. More importantly, SnS₂ could even compete with classical high refractive index materials such as Si, GaP, and TiO₂ [65–68]. In particular, SnS₂ has a wider transparency region compared with GaP and Si and a larger refractive index than TiO₂ (Figure 6). More surprisingly, when we use the refractive index from first-principle calculations (Figure 4a) for monocrystalline SnS₂, it perfectly fits into the correlation line between the refractive indices and optical bandgaps of high refractive index materials (Figure 6c). Therefore, SnS₂ enables the essential spectral range of all-dielectric nanophotonics between GaP and TiO₂.

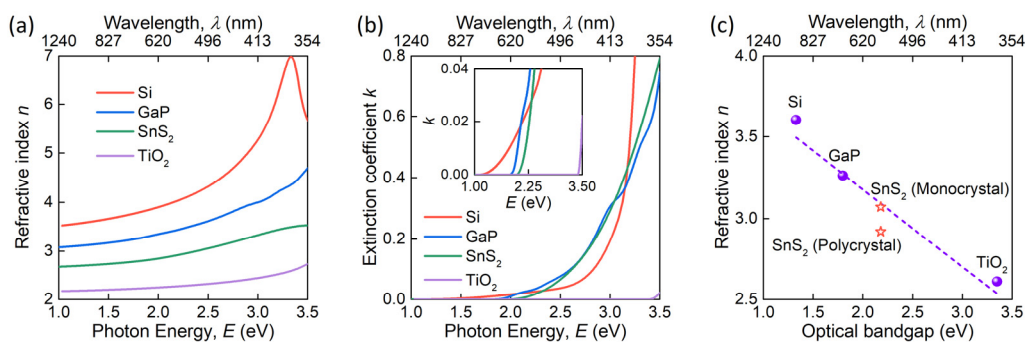


Figure 6. SnS₂ as a high refractive index material. (a) Refractive index n and (b) extinction coefficient k of SnS₂ compared with other high refractive index materials—Si, GaP, and TiO₂. (c) The dependence of refractive index and optical bandgap for high refractive index materials.

3. Materials and Methods

3.1. Materials

CVD-grown full-area coverage SnS₂ and SnSe₂ samples of thin films were purchased from 2d Semiconductors Inc. (2d Semiconductors Inc., Scottsdale, AZ, USA). The samples with an area of 1×1 cm² were grown by CVD on sapphire substrates and subsequently transferred on quartz substrates.

3.2. Surface Morphology Characterization

The surface morphology of SnS₂ and SnSe₂ thin films was analysed by an optical microscope (Nikon LV150, Tokyo, Japan) with a digital camera DS-Fi3, as well as the

scanning electron microscope (SEM) using the acceleration voltage of 30 kV and different magnifications (JEOL JSM-7001F, Tokyo, Japan) to prove films homogeneity. The film surface morphology was studied by atomic force microscopy (AFM, notegra, Nt-MDT Spectrum Instruments, Moscow, Russia) in semi-contact mode using a silicon tip with a radius <10 nm and resonance frequency of ~250 kHz (HA_NC Etalon, Tipsnano, Tallinn, Estonia) to determine surface roughnesses and films thicknesses.

3.3. Crystal Structure Characterization

X-ray diffraction (XRD) characterization was performed by X-ray diffractometer (ARL X'TRA, Thermo Fisher Scientific, Waltham, MA, USA) using Cu K_{α1} radiation line ($\lambda = 1.54 \text{ \AA}$) to analyze the crystal structure of the films using a regime of 2θ -scan with angles range of 5° – 75° with a step of 0.05° and accumulation time of 2 s.

3.4. Raman Characterization

The Raman spectra were measured with a confocal scanning Raman microscope Horiba LabRAM HR Evolution (HORIBA Ltd., Kyoto, Japan) with 532 nm linearly polarized excitation laser, 1800 lines/mm diffraction grating, and $\times 100$ objective (N.A. = 0.90) using a spectra range of 100 – 450 cm^{-1} . The spectra were recorded with 3.5 mW incident laser power, with an integration time of 10 s and 10 spectra accumulation.

3.5. Ellipsometry Analysis

The optical constants n and k of SnS₂ and SnSe₂ were measured using a variable-angle spectroscopic ellipsometer (VASE, J.A. Woollam Co., Lincoln, NE, USA), working at room temperature, at variable incidence angles 30° – 75° with a step of 5° and wide spectral range from 300 to 3300 nm with a step of 1 nm, having the spotlight of size ~1 mm around the center of the sample, utilizing the high precision optical alignment. To fit the measured ellipsometric parameters Ψ and Δ , we used the Tauc–Lorentz oscillator model was used, defined by the following formula:

$$\varepsilon_2 = \begin{cases} \frac{1}{E} \cdot \frac{AE_0C(E-E_g)^2}{(E^2-E_0^2)^2+C^2E^2} & \text{for } E > E_g \\ 0 & \text{for } E < E_g \end{cases}, \quad (2)$$

where E is the energy of the photon, A is the oscillator strength, C is the oscillator broadening, E_g is the optical band-gap, E_0 is the oscillator central energy, and the real part of the dielectric function ε_1 was obtained from the imaginary part ε_2 using the Kramers–Kronig integration, plus ε_∞ , to account for high energy electronic transitions. For SnS₂, we used one Tauc–Lorentz oscillator with the following parameters: $A = 54.613 \text{ eV}$; $C = 1.626 \text{ eV}$; $E_0 = 3.911 \text{ eV}$; $E_g = 1.970 \text{ eV}$ and $\varepsilon_\infty = 5.031$. For SnSe₂, we used two Tauc–Lorentz oscillators with the following parameters: $A_1 = 14.435 \text{ eV}$; $C_1 = 1.345 \text{ eV}$; $E_{01} = 2.870 \text{ eV}$; $A_2 = 20.432 \text{ eV}$; $C_2 = 0.875 \text{ eV}$; $E_{02} = 3.981 \text{ eV}$; $E_g = 0.736 \text{ eV}$ and $\varepsilon_\infty = 4.445$.

3.6. Optical Properties Characterization

Optical transmittance spectra of SnS₂ and SnSe₂ films on quartz were measured with a spectrophotometer (Cary 5000 UV-Vis-NIR, Agilent Tech., Santa Clara, CA, USA) at a wavelength range of 300–3300 nm.

The nonlinear optical properties of the sample were studied by a home-built multi-photon microscope [69], based on femtosecond Ti:sapphire laser (Coherent Chameleon Ultra 2, Santa Clara city, CA, USA) tunable in the spectral range from 680 to 1080 nm. The laser beam (80 MHz repetition rate, 150 fs pulse duration) was directed through the system, consisting of a half-wave plate on a motorized rotation stage and a Glan–Taylor prism, which provided control of the power and polarization of the incident radiation.

Then, the beam was focused on the sample surface with a 10 cm lens into a 50 μm spot. The sample was mounted on a 3-axis motorized stage (SigmaKoki, Tokyo, Japan) with a

minimum step of 0.1 μm , which made it possible to accurately align the sample relative to the pump spot. The SH radiation generated by the sample was collected by an objective lens (N.A. = 0.95, 100x, Olympus, Tokyo, Japan) and directed to the detection channel consisting of a tube lens, filter (FGB39 Thorlabs, Newton, NJ, USA) to cut off the pump radiation, monochromator, and a scientific CCD camera (Andor Clara, Belfast, United Kingdom). The SH signal was normalized over spectral functions of all optical elements in the detection channel including objective lens transmittance and detector sensitivity spectra. SHG spectra were measured at the same pump intensity for all wavelengths. The experimental setup was fully automated and situated in a black box.

3.7. First-Principle Calculations

The optical properties of SnS_2 and SnSe_2 were calculated using density functional theory (DFT) implemented in the Vienna Ab Initio Simulation Package [70,71]. Core electrons, their interaction with valence electrons, and exchange correlation effects were described within generalized gradient approximation [72] (Perdew–Burke–Ernzerhof functional) and the projector-augmented wave pseudopotentials [73]. The unit cell parameters were $a = b = 3.6486 \text{ \AA}$ and $c = 5.8992 \text{ \AA}$ for SnS_2 and $a = b = 3.811 \text{ \AA}$ and $c = 6.137 \text{ \AA}$ for SnSe_2 . The calculation was performed in two steps: first, the atomic positions of SnS_2 and SnSe_2 were relaxed until the interatomic forces were less than 10^{-3} eV/\AA , and a 1-electron basis set was obtained from a standard DFT calculations. Second, the real and imaginary parts of frequency-dependent dielectric function were calculated using the GW approximation [74]. Cutoff energy of the plane waves basis set was set to 600 eV, and the Γ -centered $11 \times 11 \times 7$ k-points mesh was used to sample the first Brillouin zone.

4. Conclusions

In conclusion, we theoretically and experimentally determined the anisotropic optical constants of SnS_2 and SnSe_2 in a wide spectral range (300–3300 nm). Our findings reveal a strong dielectric response of SnS_2 and SnSe_2 and their broad range with zero absorption. More importantly, for SnS_2 , this range includes visible frequencies, which makes SnS_2 a novel high refractive index material, which complements the classical high refractive index materials Si, GaP, and TiO_2 . Additionally, we measured the second-order nonlinear susceptibility of SnS_2 and SnSe_2 . From a broader perspective, our research enables a foundation for advanced optical engineering with SnS_2 and SnSe_2 .

Author Contributions: V.S.V., A.V.A., A.A.F. and A.A.V. suggested and directed the project; G.A.E., D.I.Y., M.A.E.-S., M.K.T., A.A.P., I.M.A., V.O.B., A.S.S., G.I.T. and S.M.N. performed the measurements and analyzed the data; A.B.M. and I.A.K. provided theoretical support; G.A.E., D.I.Y., M.A.E.-S., M.K.T., A.A.V., A.V.A. and V.S.V. interpreted the experimental results; G.A.E., D.I.Y. and M.A.E.-S. wrote the original draft; G.A.E., D.I.Y., A.A.V., A.V.A. and V.S.V. reviewed and edited the paper; G.A.E., D.I.Y. and M.A.E.-S. contributed equally to this work and should be considered the first co-authors. All authors contributed to the discussions and commented on the paper. All authors have read and agreed to the published version of the manuscript.

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Conflicts of Interest: The authors declare no conflict of interest.

Appendix A

Table A1. Tabulated optical constants for SnS₂ and SnSe₂ films from Figure 3a,b.

λ (nm)	SnS ₂		SnSe ₂	
	n	k	n	K
300	3.8943	1.0436	2.8895	2.5984
350	3.5319	0.8434	3.8561	1.3915
400	3.3828	0.3664	3.5830	1.1143
450	3.1896	0.1537	3.6856	0.9836
500	3.0450	0.0599	3.7271	0.7105
550	2.9415	0.0180	3.6563	0.4900
600	2.8674	0.0021	3.5609	0.3480
650	2.8171	0.0000	3.4737	0.2566
700	2.7841	0.0000	3.4004	0.1950
750	2.7602	0.0000	3.3399	0.1515
800	2.7420	0.0000	3.2897	0.1195
850	2.7277	0.0000	3.2477	0.0952
900	2.7163	0.0000	3.2122	0.0762
1200	2.6782	0.0000	3.0787	0.0190
1500	2.6621	0.0000	3.0115	0.0021
1800	2.6537	0.0000	2.9751	0.0000
2100	2.6488	0.0000	3.6446	0.0000
2400	2.6456	0.0000	3.6001	0.0000
2700	2.6434	0.0000	3.5663	0.0000
3000	2.6419	0.0000	3.5400	0.0000
3300	2.6408	0.0000	3.5194	0.0000

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